

Sec. 3.3 Skills Refresher: Quadratic Equations

Distributive Property: For real numbers a, b, and c we can simplify:

$$a(b + c) = ab + ac$$

Ex. Simplify the following expressions:

a. $3x^2(x + \frac{1}{6}x^{-3})$

$$\begin{aligned} &3x^3 + \frac{1}{2}x^{-1} \\ &3x^3 + \frac{1}{2}x \end{aligned}$$

b. $((2t)^2 - 5) * \sqrt{t}$

$$\begin{aligned} &4t^2 \cdot t^{\frac{1}{2}} - 5t^{\frac{1}{2}} \\ &4t^{\frac{5}{2}} - 5t^{\frac{1}{2}} \\ &4t^{\frac{5}{2}} - 5t^{\frac{1}{2}} \end{aligned}$$

c. $(5x^2 + 2)(x - 4)$

$$5x^3 - 20x^2 + 2x - 8$$

d. $(2\sqrt{t} + 2)(4\sqrt{t} - 3)$

$$\begin{aligned} &8t - 3\sqrt{t} + 8\sqrt{t} - 6 \\ &8t + 5\sqrt{t} - 6 \end{aligned}$$

e. $(3 - \frac{1}{2}x)^2$

$$\begin{aligned} &(3 - \frac{1}{2}x)(3 - \frac{1}{2}x) \\ &9 - \frac{3}{2}x - \frac{3}{2}x + \frac{1}{4}x^2 \\ &9 - \frac{6}{2}x + \frac{1}{4}x^2 \end{aligned}$$

$$9 - 3x + \frac{1}{4}x^2$$

Adding and Subtracting Polynomials

**Group like terms and then combine them.

Ex. $8x^3 - 2x^2 + 6x - 2$ and $3x^4 - 2x^3 + x^2 + x$

Add: $3x^4 + 6x^3 - x^2 + 7x - 2$

Subtract: $-3x^4 + 10x^3 - 3x^2 + 5x - 2$

Multiplying Polynomials

**Use laws of exponents and Distributive property.

Ex. $(2x + x^3) * (5x - 3 + 2x^4) =$

$$\begin{aligned} &10x^2 - 6x + 4x^5 + 5x^4 - 3x^3 + 2x^7 \\ &2x^7 + 4x^5 + 5x^4 - 3x^3 + 10x^2 - 6x \end{aligned}$$

Factoring Polynomials

There are many ways to factor polynomials depending on their equations. Some possibilities are:

1. Removing a Common Factor $ab + ac = a(b + c)$
2. Grouping Terms $x^2 - hx - x + h = (x^2 - hx) - (x - h) = x(x - h) - (x - h) = (x - h)(x - 1)$
3. Factoring Quadratics (multiples of c that add to b)
4. Perfect Squares and Differences of Squares
 - a. $a^2 + 2ab + b^2 = (a + b)^2$
 - b. $a^2 - 2ab + b^2 = (a - b)^2$
 - c. $a^2 - b^2 = (a - b)(a + b)$
5. Quadratic Formula
6. Zero Product Property
If $ab = 0$ then either $a = 0$ or $b = 0$.

Review: Solving Equations (remember you can use one variable method, factoring, square root method, completing the square method, or the quadratic formula)

$$1. \frac{x^2 - 4}{x + 1} = 3$$

$$\begin{aligned} x^2 - 4 &= 3(x+1) \\ x^2 - 4 &= 3x + 3 \\ x^2 - 3x - 7 &= 0 \\ +3 \pm \sqrt{(-3)^2 - 4(1)(-7)} &= 2(1) \end{aligned}$$

$$2. \sqrt{(3x-5)^2} = \sqrt{14}$$

$$\begin{aligned} 3x - 5 &= 2 & 3x - 5 &= -2 \\ 3x &= 7 & 3x &= 3 \\ x &= \frac{7}{3} & x &= 1 \end{aligned}$$

$$3. x^2 = 4x$$

$$\begin{aligned} x^2 - 4x &= 0 \\ x(x-4) &= 0 \\ x = 0 & \quad x-4 = 0 \\ x &= 4 \end{aligned}$$

$$4. x^3 - x^2 - 4x + 4 = 0$$

$$\begin{aligned} x^2(x-1) - 4(x-1) &= 0 \\ (x-1)(x^2-4) &= 0 \\ (x-1)(x+2)(x-2) &= 0 \\ x-1=0 & \quad x+2=0 & \quad x-2=0 \\ x=1 & \quad x=-2 & \quad x=2 \end{aligned}$$

$$5. x^2 + 5 = 30$$

$$\begin{aligned} x^2 &= 25 \quad \text{or} \quad x^2 - 25 = 0 \\ x &= \pm 5 \quad (x+5)(x-5) = 0 \\ x+5 &= 0 & x-5 &= 0 \\ x &= -5 & x &= 5 \end{aligned}$$

$$6. (x+3)^2 = 36$$

$$\begin{aligned} x+3 &= 6 & x+3 &= -6 \\ x &= 3 & x &= -9 \end{aligned}$$

$$7. 5x^2 + 3x + 1 = 0$$

$$\begin{aligned} 5x^2 + 3x - 2 &= 0 \\ (5x+2)(x-1) &= 0 \\ 5x+2 &= 0 & x-1 &= 0 \\ 5x &= -2 & x &= 1 \\ x &= -\frac{2}{5} & \boxed{x=1} \end{aligned}$$

$$8. (x+3)(2x-5) = 0.$$

$$\begin{aligned} x+3 &= 0 & 2x-5 &= 0 \\ x &= -3 & 2x &= 5 \\ x &= \frac{5}{2} & x &= 2\frac{1}{2} \end{aligned}$$

HW: pg 123 -125 #3 – 93 (m/3)